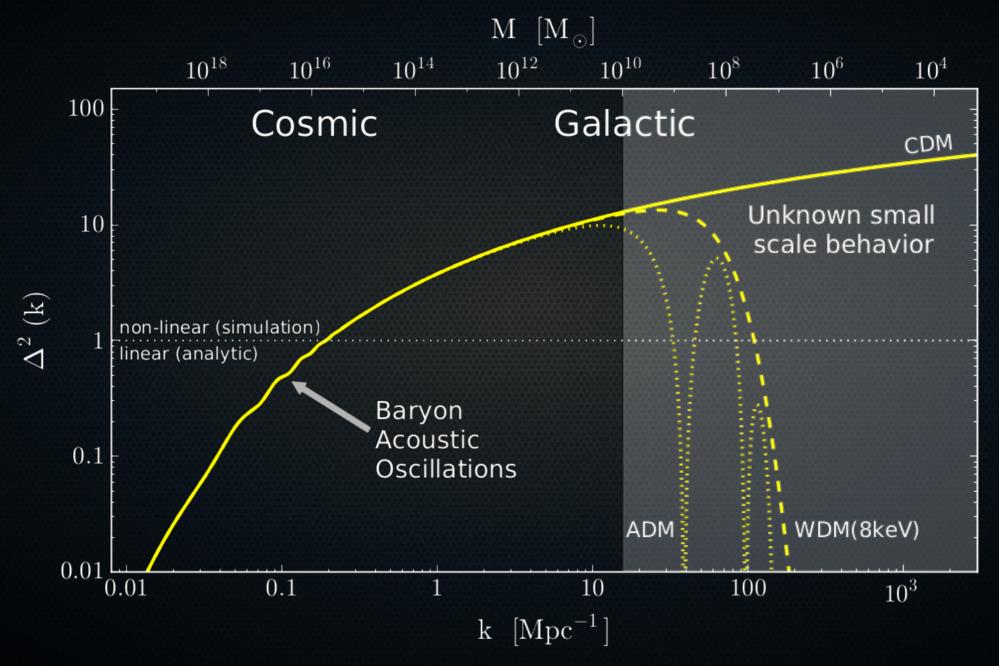
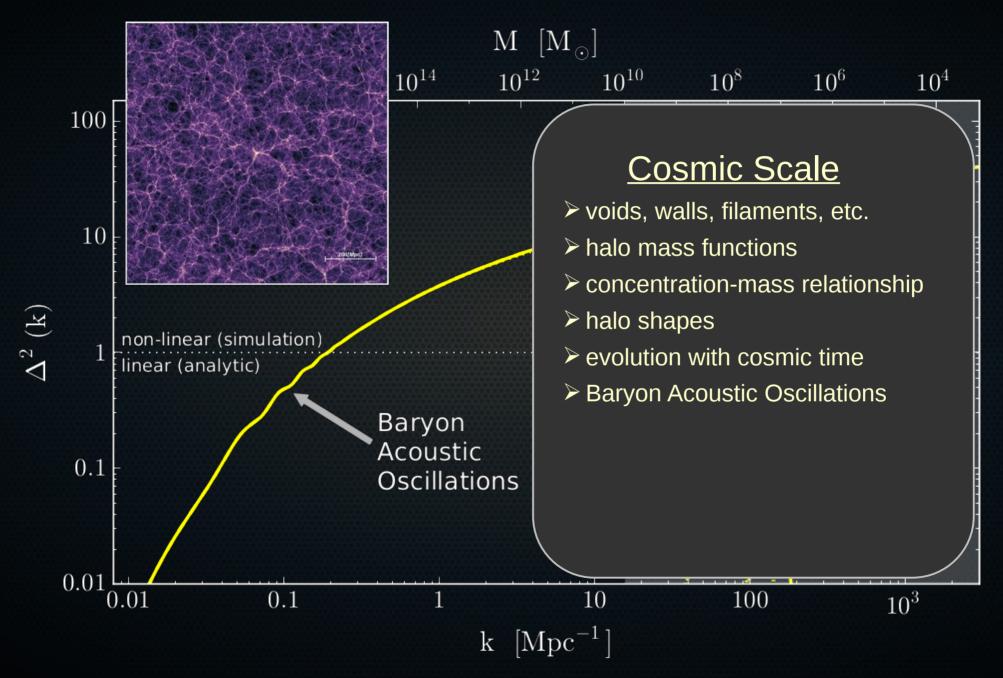
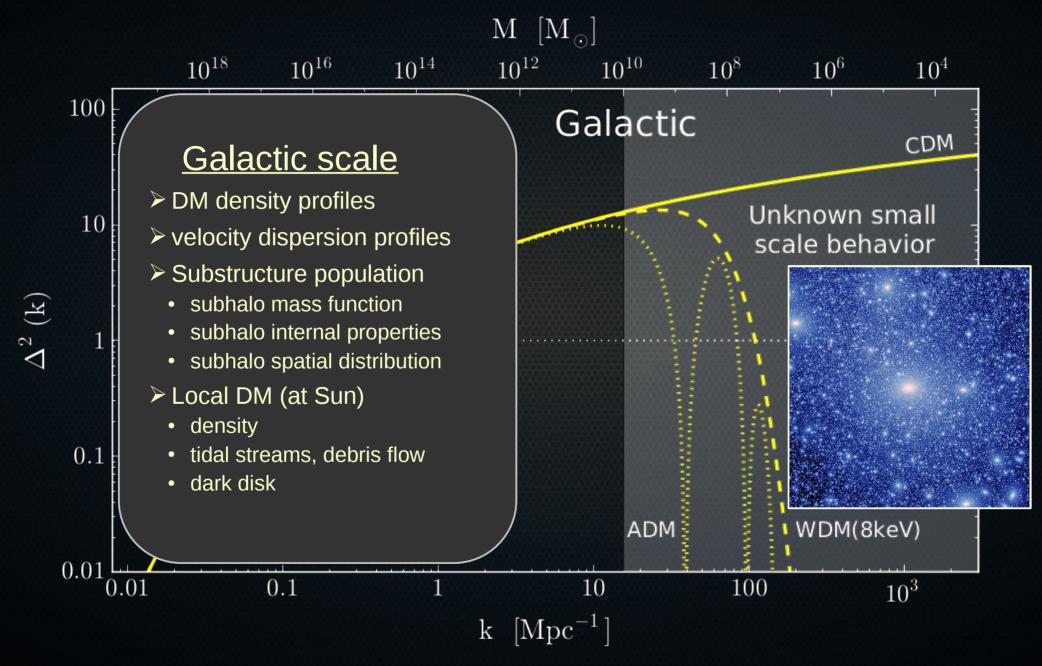
# Most Matter is Dark Matter, but that's not all that matters.

Michael Kuhlen, Berkeley

With J. Diemand (Zurich), J. Guedes (Zurich), M. Lisanti (Princeton), P. Madau (UC Santa Cruz), L. Mayer (Zurich), A. Pillepich (UC Santa Cruz), N. Weiner (NYU), A. Brooks (U. Wisconsin), A. Zolotov (Hebrew U. Jerusalem)



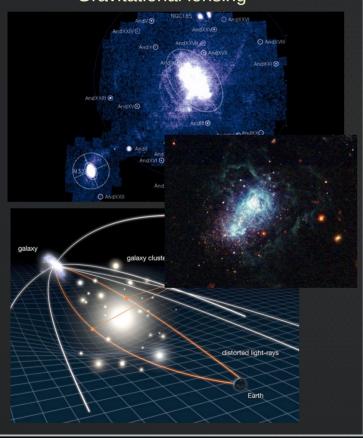




## **Dark Matter Detection Applications**

#### **Astro-physical Probes**

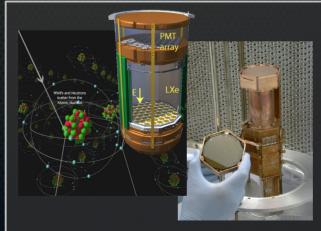
- Dwarf galaxy census
- Stellar kinematics
- Stellar streams
- > Gravitational lensing





#### <u>Indirect Detection</u> (<u>Annihilation</u>)

- Extra-galactic DGRB
- Galactic DGRB
- Clusters
- Galactic Center
- Milky Way Dwarfs
- Dark Subhalos
- > e+/e- from local annihilation
- Neutrinos from Earth & Sun
- "Boost factor"

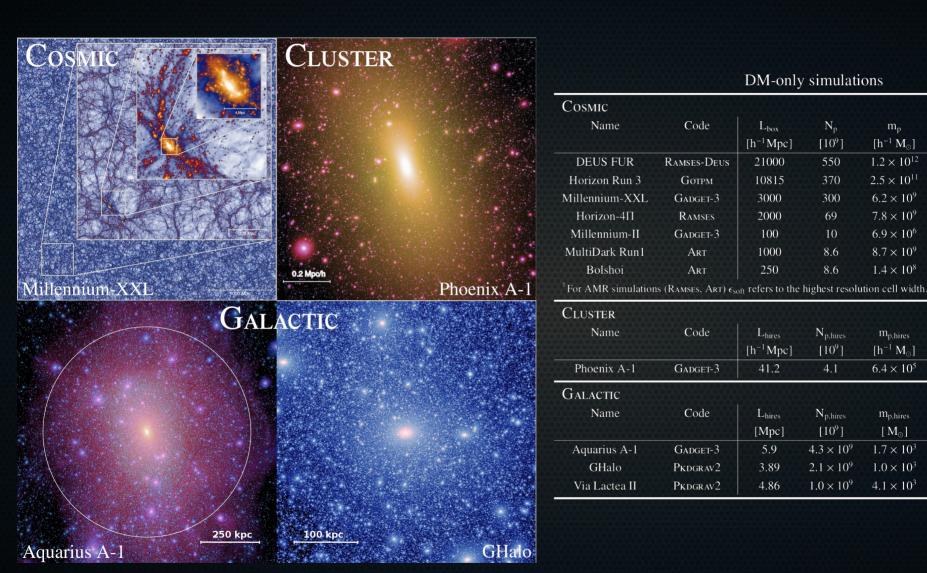


#### <u>Direct Detection</u> (Nuclear Recoils)

- standard case: "vanilla" WIMPs
- low mass DM, inelastic DM, etc.
- directionally sensitive experiments

		LSS		Halos				Substructure						I	Local		
From Kuhlen, Vogelsberger & Angulo 2012 (arXiv:1209.5745)		voids, walls, filaments	halo mass functions	concentration-mass relation	halo shapes	density profiles	pseudo-phase-space density	mass (or V <sub>max</sub> ) functions	density profiles	central density	spatial distribution	streams	folds & caustics	local density	tidal streams	dark disk	
Astrophysical	Dwarf galaxy abundance																
	Dwarf galaxy kinematics						200000					11111					
	Stellar streams														93300	jiji.	
	Gravitational lensing															##	
on	Extra-galactic DGRB																
	Galactic DGRB																
cti	Clusters																
Indirect Detection	Galactic Center																
	Milky Way Dwarfs																
	Dark Subhalos																
	Local anti-matter		2000														
pu	Neutrinos from Earth & Sun		2000							20000							
	Substructure boost					100000									<b>AND</b>		
	Sommerfeld boost																
+	"Vanilla" ~ 100 GeV DM																
Direct	light / inelastic DM																
Dii	axions	T C C C C C C C C C C C C C C C C C C C															
	directionally sensitive experiments																

#### **Current State Of The Art**



Kuhlen, Vogelsberger & Angulo 2012 (arXiv:1209.5745)

 $\epsilon_{
m soft}$ 

 $[h^{-1}kpc]$ 

 $40.0^{\dagger}$ 

150.0

10.0

 $7.6^{\dagger}$ 

1.0

7.6

 $1.0^{\dagger}$ 

 $[h^{-1}kpc]$ 

0.15

 $\epsilon_{
m soft}$ 

[pc]

20.5

61.0

40.0

 $[10^6]$ 

145

~ 190

170

~40

2.3

3.3

2.4

 $[10^3]$ 

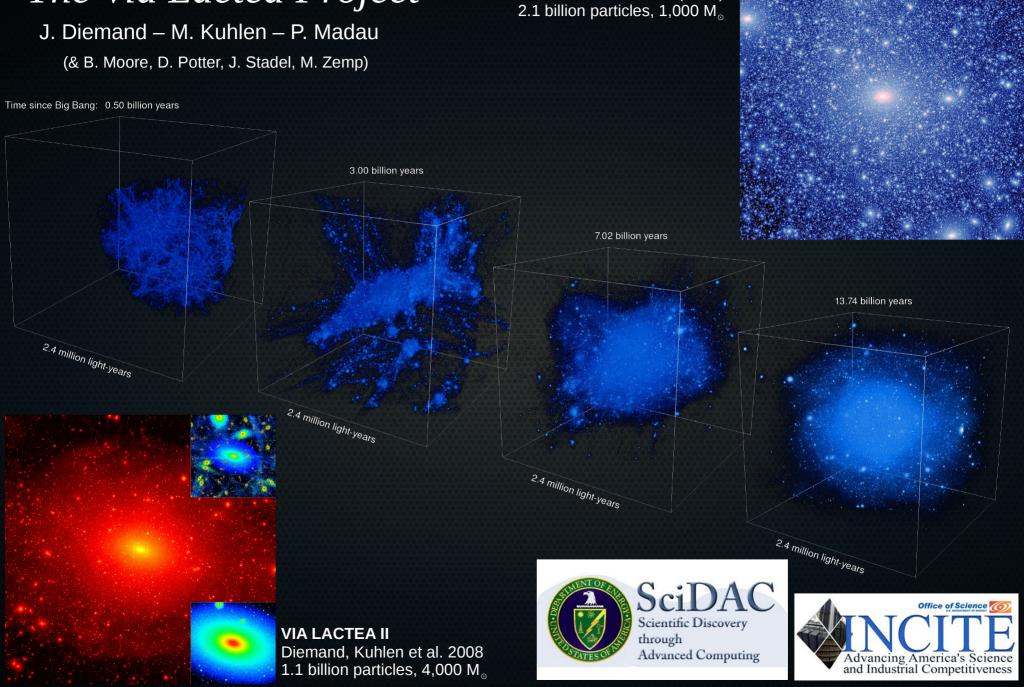
60

 $N_{\text{sub}}^{>100p}$ 

 $[10^3]$ 

82

## The Via Lactea Project



**GHALO** 

Stadel et al. (2009)

## The Via Lactea Project

J. Diemand – M. Kuhlen – P. Madau (& B. Moore, D. Potter, J. Stadel, M. Zemp)



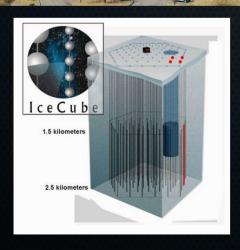
VIA LACTEA II (1.1 billion particles, 4,000  ${\rm M}_{\odot}$ )

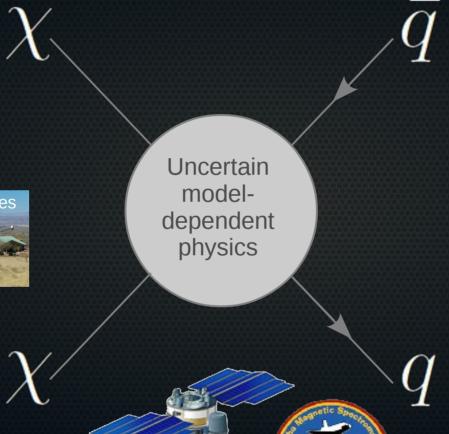


Annihilation sets the abundance of dark matter in the early universe. Possibly detectable signal from DM concentrations in the present.

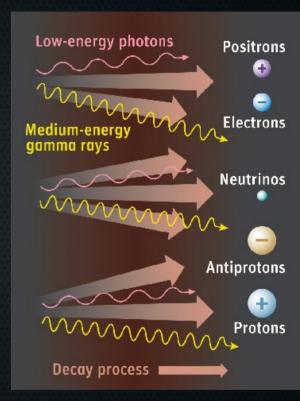


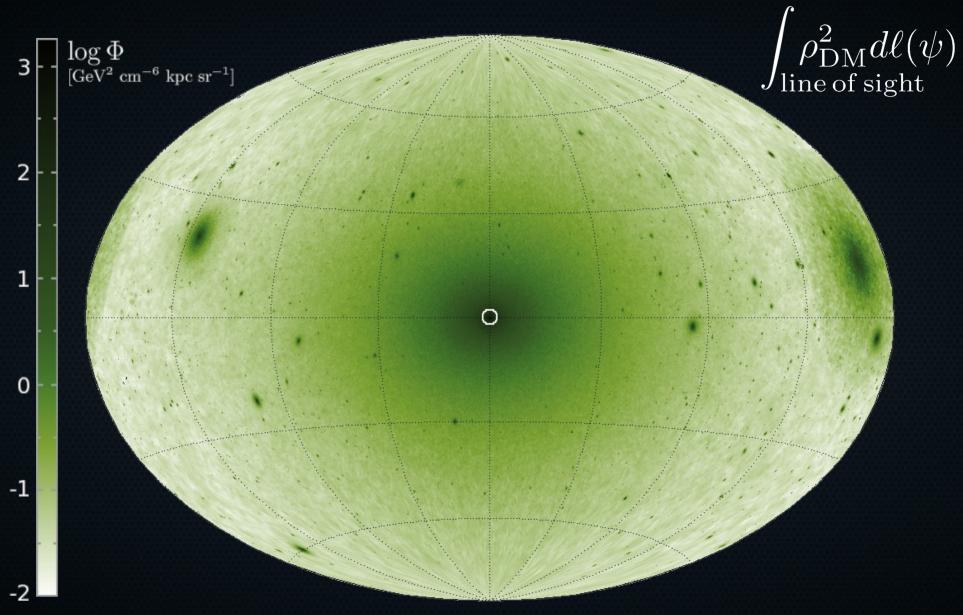
Atmospheric Cerenkov Telescopes





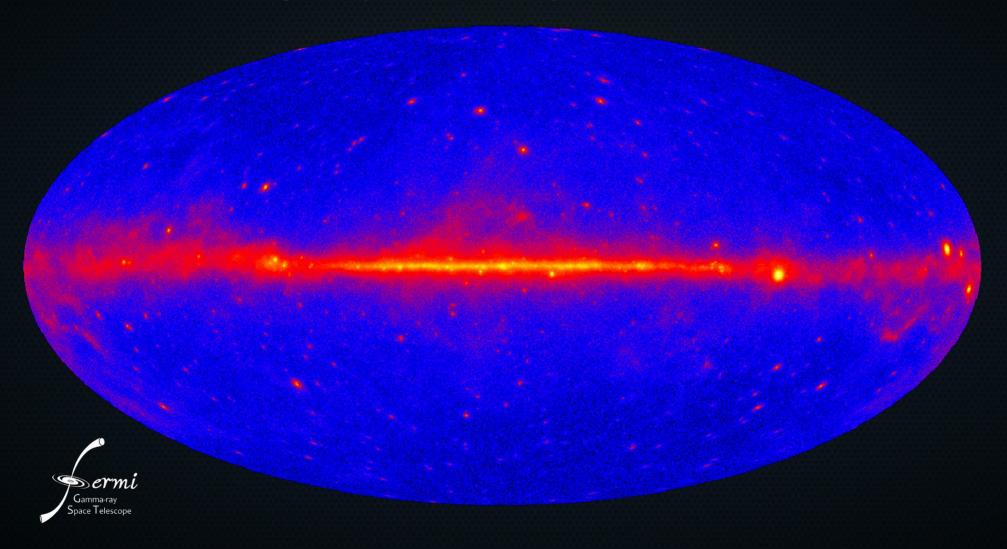
PAMELA satellite



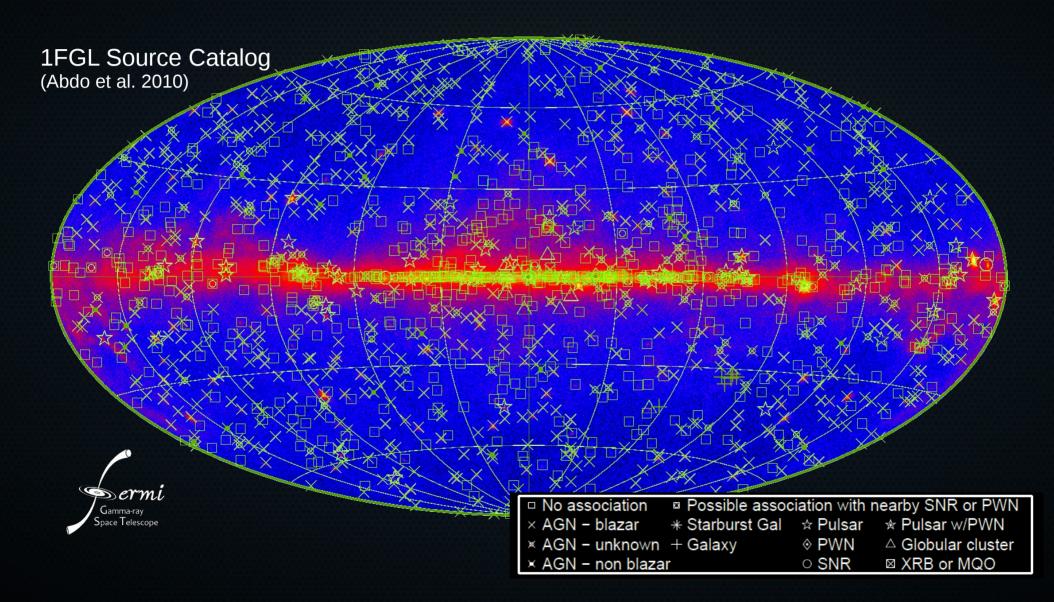


Kuhlen, Diemand, & Madau (2008)

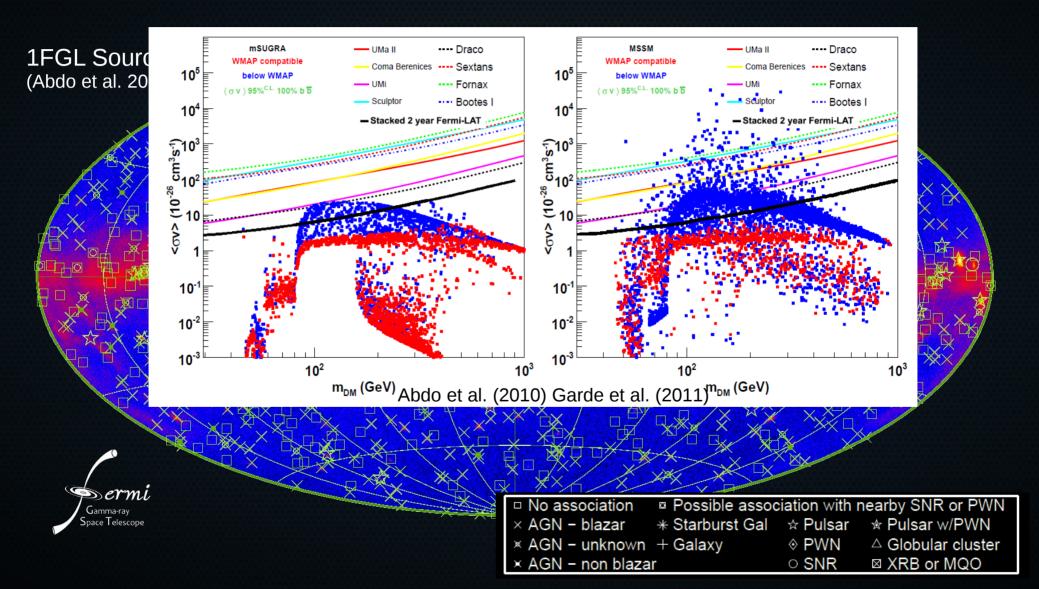
The Fermi Gamma-ray Space Telescope was launched on June 11<sup>th</sup> 2008 and has been observing the sky for more than 4 years.

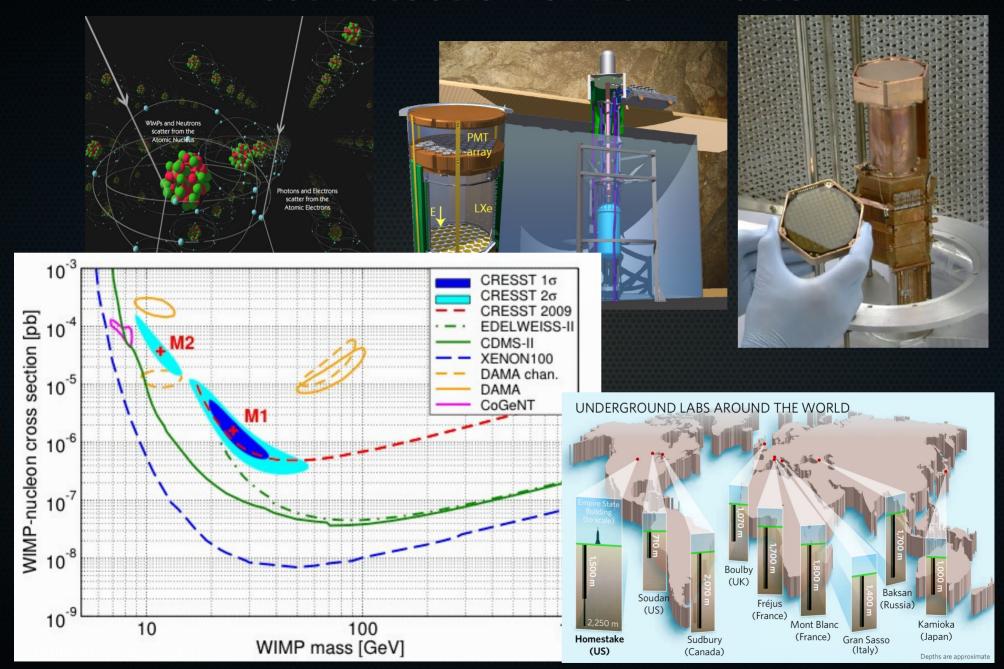


So far, no dark matter signal has been detected. Stay tuned...



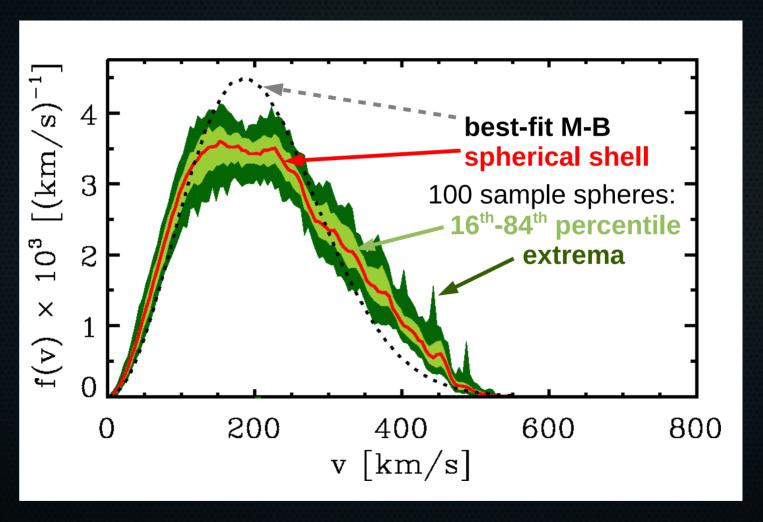
So far, no dark matter signal has been detected. 😊 Stay tuned...





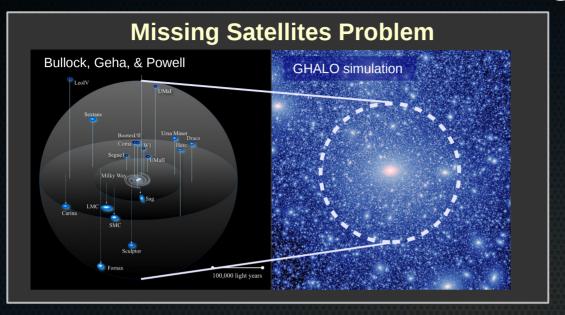
## I. Velocity Substructure and Direct Detection

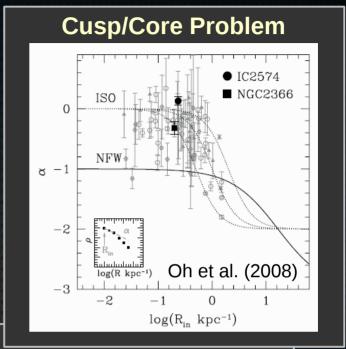
$$\frac{dR}{dE_R} = N_T M_N \frac{\rho_{\chi} \sigma_n}{2m_{\chi} \mu_{ne}^2} \frac{(f_p Z + f_n (A - Z))^2}{f_n^2} F^2[E_R] \int_{\beta_{min}}^{\infty} \frac{f(v)}{v} dv$$

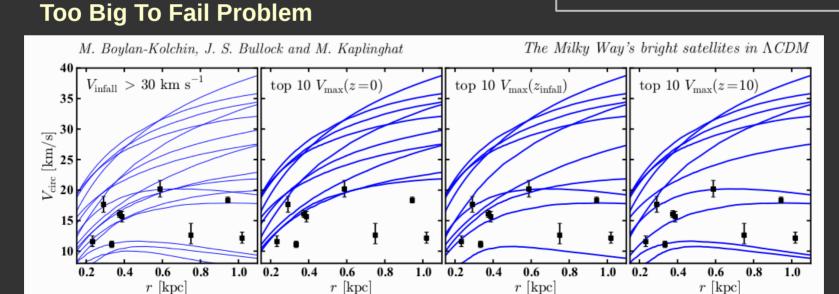


Kuhlen et al. (2010); see also Hansen et al. (2005), Vogelsberger et al. (2009)

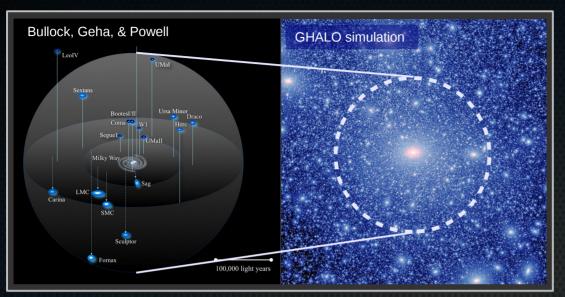
## **Small Scale Challenges for CDM**

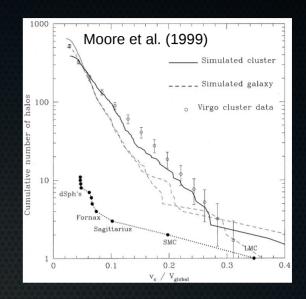


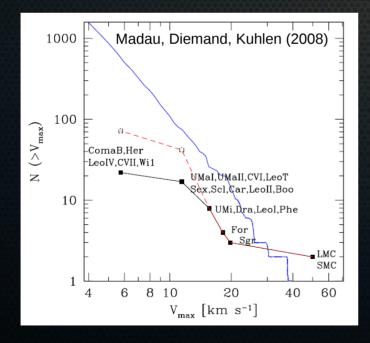


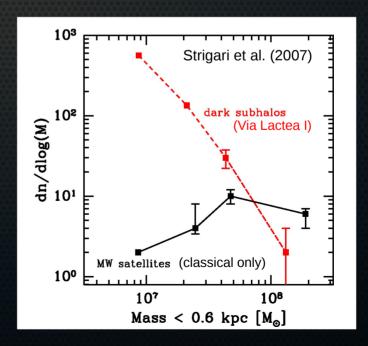


## **Missing Satellites Problem**









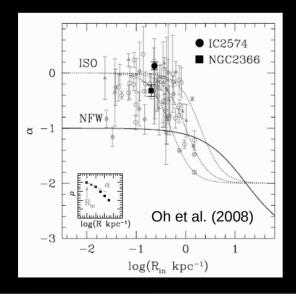
## **Cusp/Core Problem**

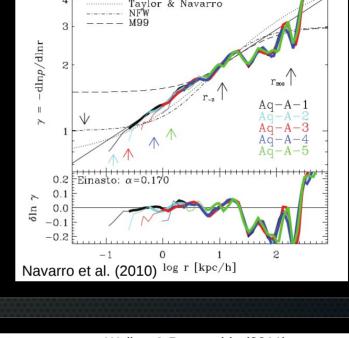
DM-only N-body simulations predict cuspy density profiles:  $\gamma \equiv -\frac{d \ln \rho}{d \ln r} \lesssim 1$ 

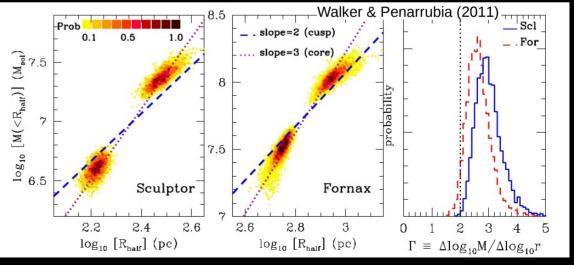
$$\rho(r) = \frac{\rho_s}{(r/r_s)(r/r_s + 1)^2} \quad (NFW)$$

$$\ln \frac{\rho(r)}{\rho_s} = -\frac{2}{\alpha} \left[ (r/r_s)^{\alpha} - 1 \right] \quad \text{(Einasto)}$$

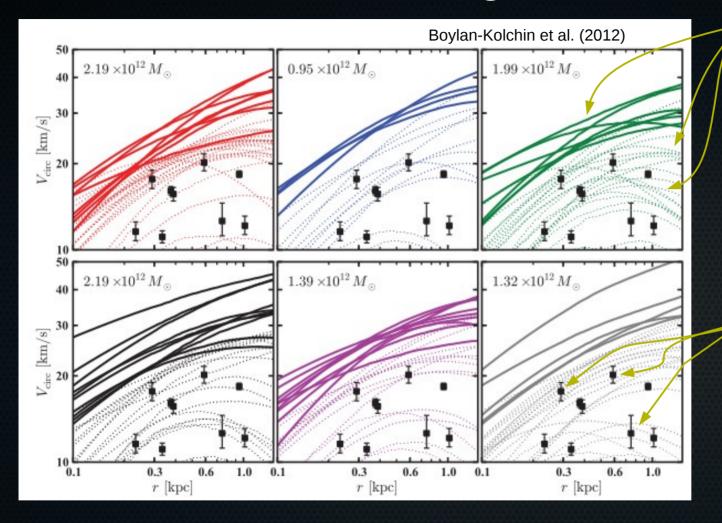
Observations in dwarf galaxies appear to prefer cores:  $\gamma \equiv -\frac{d \ln \rho}{d \ln r} \approx 0$ 







## "Too Big To Fail"



Circular velocity curves for subhalos in the six Aquarius host halos.

$$V_{\rm circ}(r) = \sqrt{\frac{G M(< r)}{r}}$$

The circular velocity at the half-light radius of the Milky Way's classical dwarf satellite galaxies determined from radial velocities of ~100's of stars each. (Wolf et al. 2010)

The DM-only simulations always contain a population of subhalos that are **too dense** or **too massive** to host any of the dwarf spheroidals with well constrained  $V_c(r_{1/2})$ .

## Beyond Cold & Collisionless DM-only Simulations

Cold and Collisionless DM-only Simulations [Millennium II, Via Lactea II, Aquarius, etc.]

#### Alternative Dark Matter Physics

Warm Dark Matter Self-Interacting Dark Matter ???

#### Include Baryonic Physics

Gas Cooling
Star Formation
Feedback

## Beyond Cold & Collisionless DM-only Simulations

Cold and Collisionless DM-only Simulations [Millennium II, Via Lactea II, Aquarius, etc.]

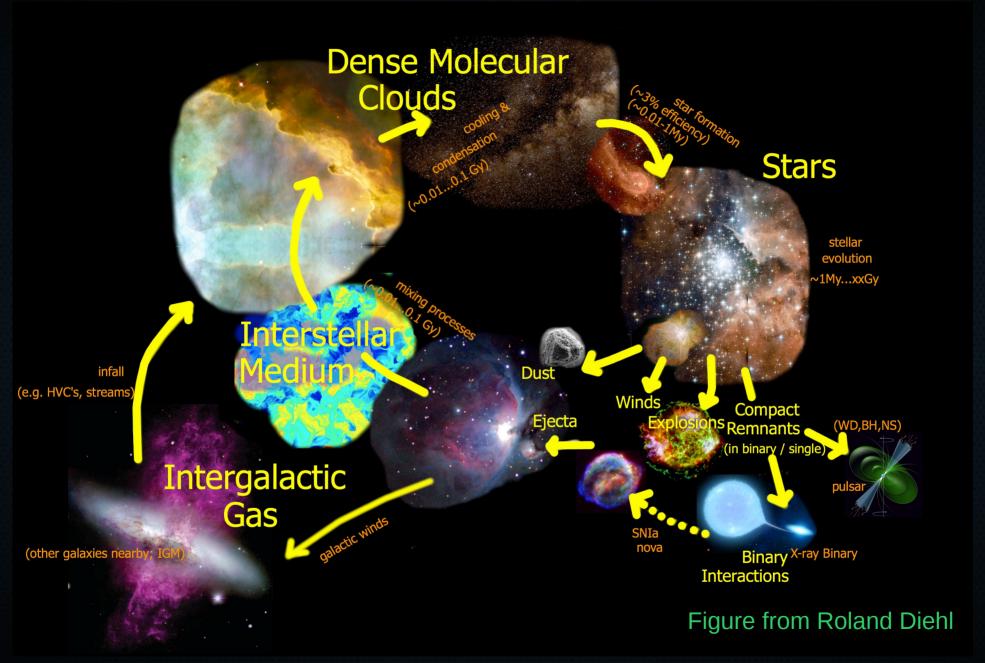
#### Alternative Dark Matter Physics

Warm Dark Matter Self-Interacting Dark Matter ???

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Gas Cooling
Star Formation
Feedback

## Beyond DM-only: including baryonic physics



## **Treatment of Hydrodynamics**

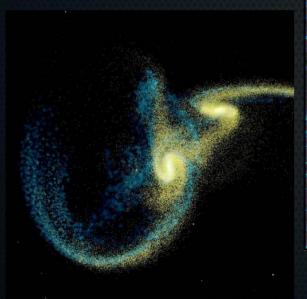
$$\frac{\partial \boldsymbol{u}}{\partial t} + \frac{\partial \boldsymbol{f}}{\partial x} = 0 \qquad \boldsymbol{u} = \begin{pmatrix} \rho \\ \rho v \\ \rho E \end{pmatrix} \qquad \boldsymbol{f} = \begin{pmatrix} \rho v \\ \rho v^2 \\ (\rho E + p)v \end{pmatrix}$$

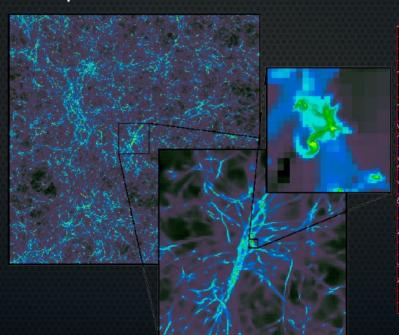
$$\frac{\partial}{\partial t} \int_{x_1}^{x_2} \boldsymbol{u} \, dx + \int_{x_1}^{x_2} \frac{\partial \boldsymbol{f}}{\partial x} dx = 0$$

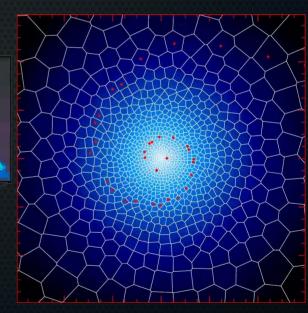
Smoothed Particle Hydrodynamics

Adaptive Mesh Refinement

**Moving Mesh** 





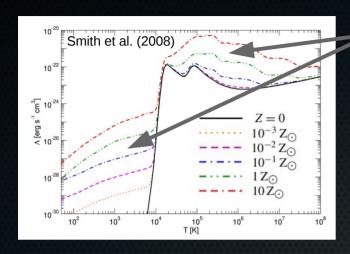


Gadget, Gasoline, ...

Enzo, H-ART, FLASH, RAMSES, ...

Arepo

## Cooling, Star Formation, Feedback...

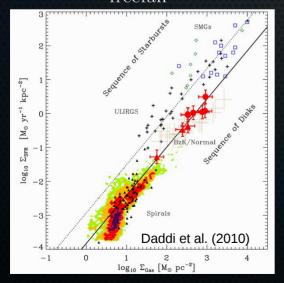


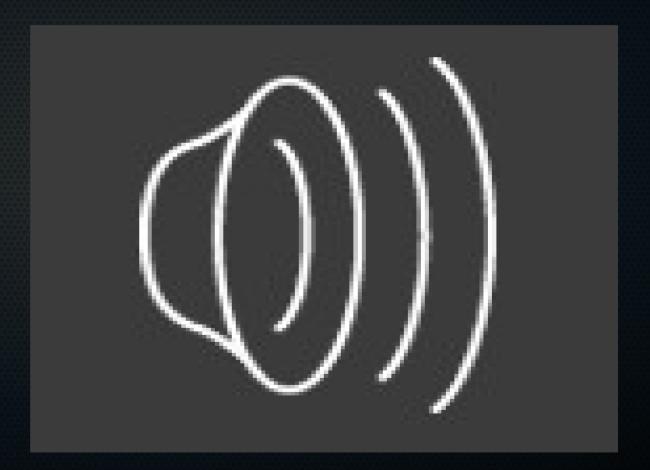
Metal-dependent cooling:  $\Lambda(T, x_e, UVB(z), Z)$ 

Supernova (and/or AGN) feeback prescription

Star Formation calibrated to Kennicutt-Schmidt relation

$$\dot{\rho}_{\rm SF} = \epsilon_{\star} \, \frac{\rho_{\rm H_2}}{t_{\rm freefall}} \propto f_{\rm H_2} \, \rho_{\rm gas}^{3/2}$$

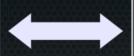




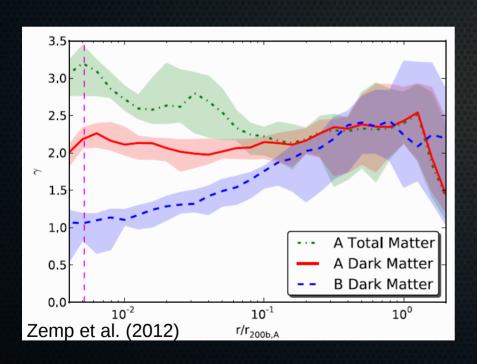
## Beyond DM-only: including baryonic physics

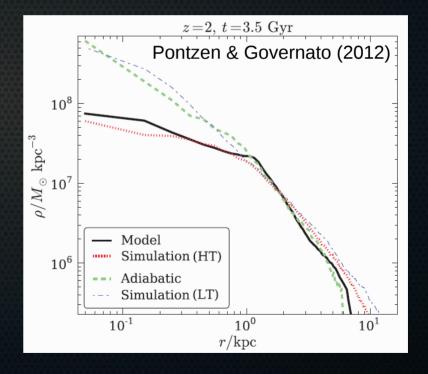
Often not even the sign of the effect is known...

Adiabatic contraction steepens the DM profile and <u>increases</u> <u>central DM densities</u>.



Impulsive supernova (or AGN) feedback <u>removes DM from the</u> <u>center</u> and flattens the DM cusp.

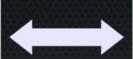




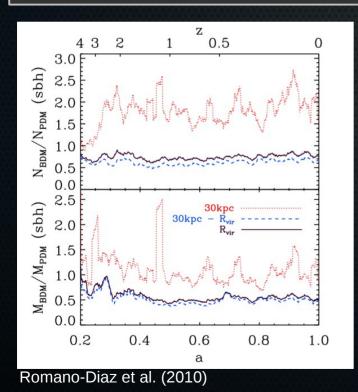
## **Beyond DM-only: including baryonic physics**

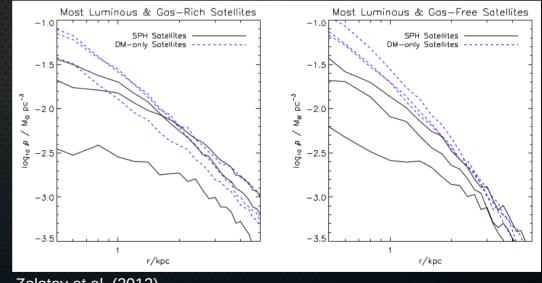
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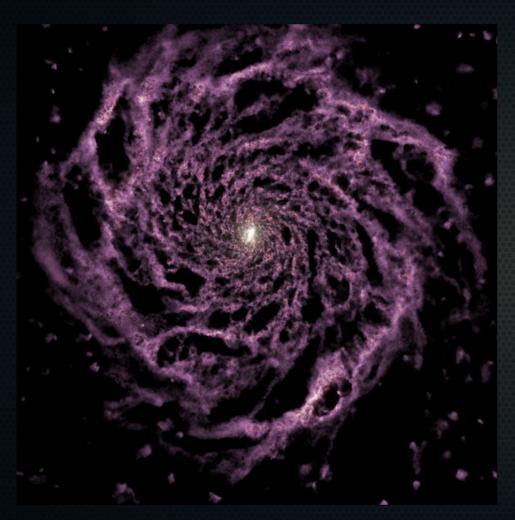
Baryonic condensation in the centers of satellite halos makes them more resilient to tidal disruption and **increases** abundance of inner subhalos.



The deeper host halo potential, satellite cusp removal, and disk passages enhance tidal stripping and reduce the number of surviving subhalos.







For more details see Guedes et al. 2011

Cosmological SPH Zoom-in Simulation

7 million DM particles ( $10^5 M_{\odot}$ )

3 million gas particles ( $2\times10^4~{\rm M}_{\odot}$ )

8.6 million star particles (4-6 $\times$ 10<sup>3</sup> M<sub> $\odot$ </sub>)

- radiative cooling (Compton, atomic, low-T metallicity-dependent)
- heating from cosmic UV(~ Haardt & Madau 1996)
- > Supernova feedback ( $\varepsilon_{SN}$ =0.8) (Stinson et al. 2006)
- Star formation
  - threshold:  $n_{SF} = 5$  atoms/cm<sup>3</sup>
  - efficiency:  $\varepsilon_{SF} = 0.1$
  - IMF: Kroupa et al. 1993
  - No AGN feedback

Results in a realistic looking Milky-Way-like spiral disk galaxy at z=0.



For more details see Guedes et al. 2011

Cosmological SPH Zoom-in Simulation

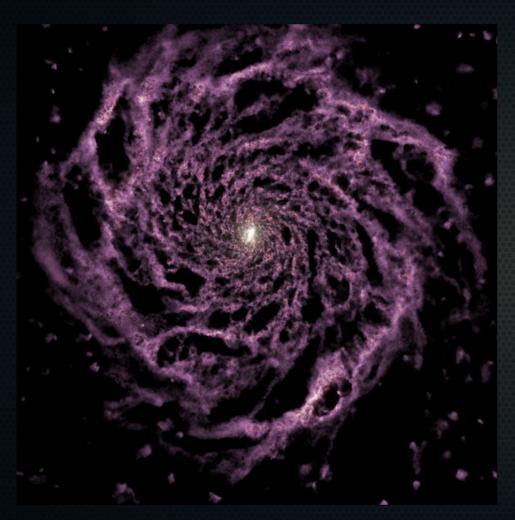
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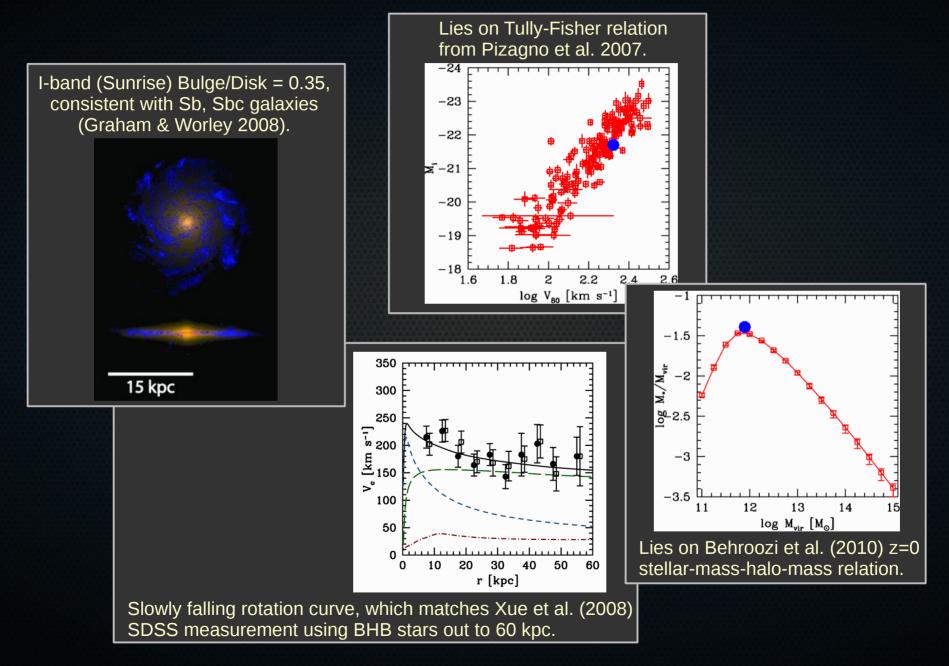
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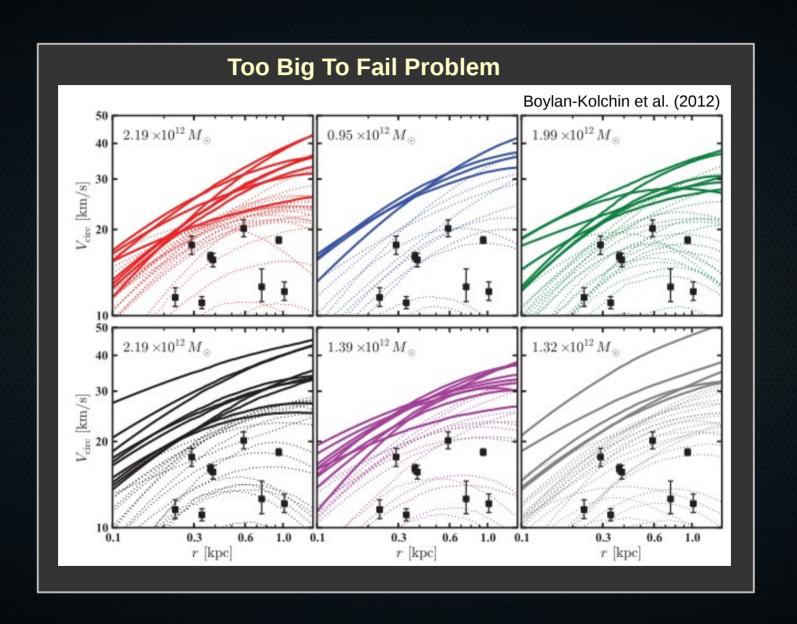


## **Baryonic Effects on Dark Matter**

#### Two Examples:

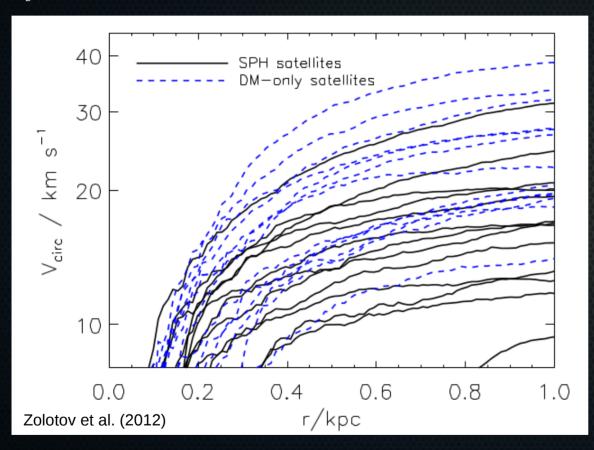
- 1) A Baryonic Solution to "Too Big To Fail" Brooks, Kuhlen, Zolotov, & Hooper (2012), arXiv:1209.5394
- 2) An Offset Dark Matter Density Peak in the Galactic Center?

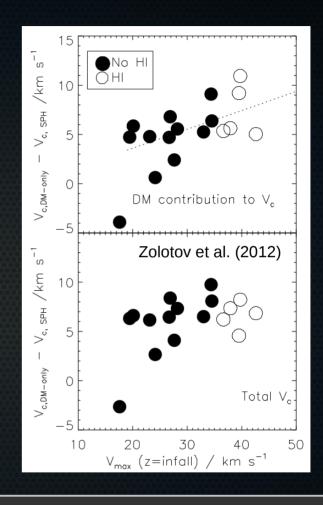
Kuhlen et al. (2012), arXiv:1208.4844



#### Simulations similar to Eris

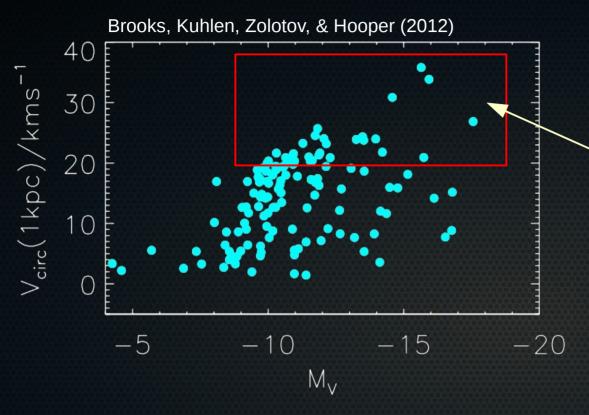
[GASOLINE SPH code, slightly poorer resolution, same feedback prescription, H<sub>2</sub>-regulated SF; see Zolotov et al. 2012 & Brooks & Zolotov 2012 for details.]





A prescription to apply to DM-only simulations:

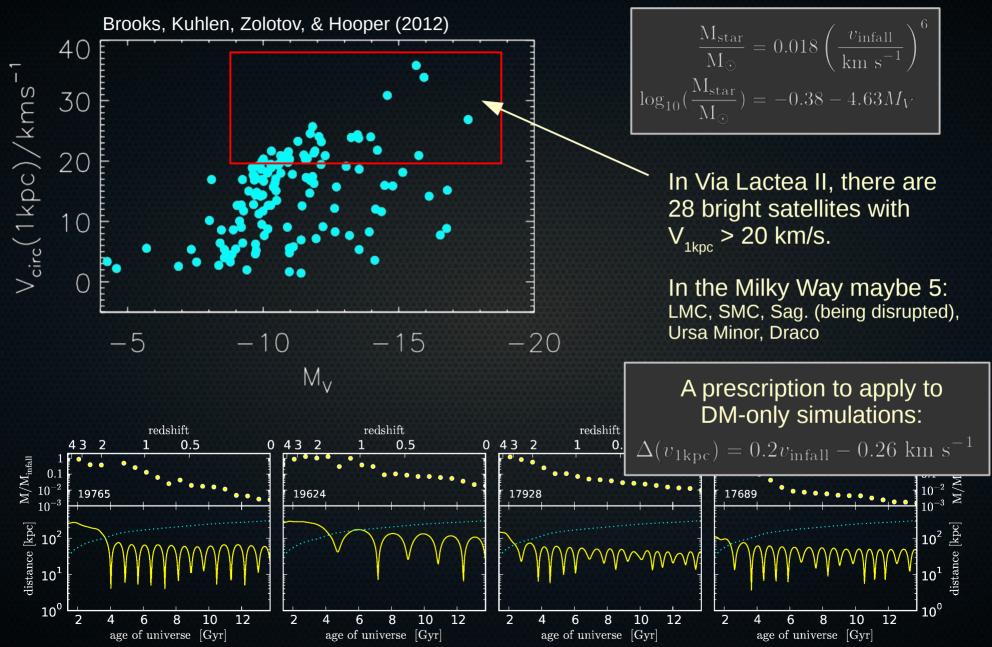
 $\Delta(v_{1 \text{kpc}}) = 0.2v_{\text{infall}} - 0.26 \text{ km s}^{-1}$ 



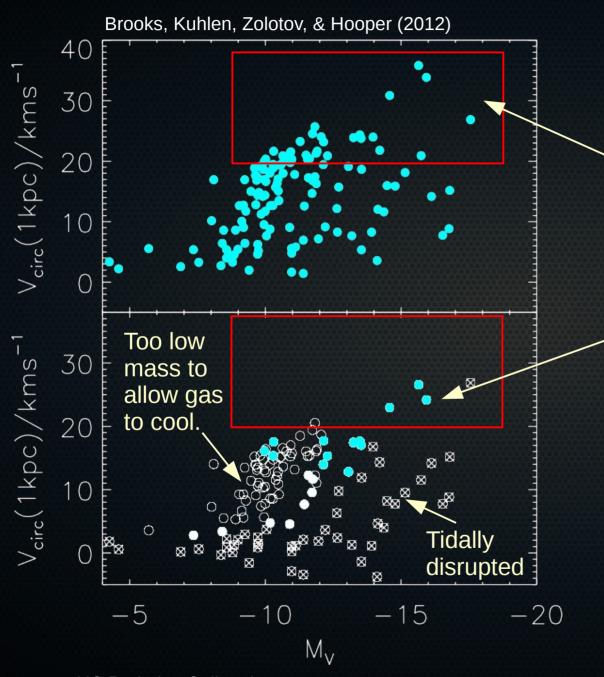
$$\frac{\mathrm{M_{star}}}{\mathrm{M}_{\odot}} = 0.018 \left(\frac{v_{\mathrm{infall}}}{\mathrm{km s}^{-1}}\right)^{6}$$
$$\log_{10}\left(\frac{\mathrm{M_{star}}}{\mathrm{M}_{\odot}}\right) = -0.38 - 4.63 M_{V}$$

In Via Lactea II, there are 28 bright satellites with  $V_{1kpc} > 20$  km/s.

In the Milky Way maybe 5: LMC, SMC, Sag. (being disrupted), Ursa Minor, Draco



### II. A Baryonic Solution to Too Big To Fail



$$\frac{\mathrm{M_{star}}}{\mathrm{M}_{\odot}} = 0.018 \left(\frac{v_{\mathrm{infall}}}{\mathrm{km s}^{-1}}\right)^{6}$$
$$\log_{10}\left(\frac{\mathrm{M_{star}}}{\mathrm{M}_{\odot}}\right) = -0.38 - 4.63 M_{V}$$

In Via Lactea II, there are 28 bright satellites with  $V_{1kpc} > 20$  km/s.

Number of satellites agrees with obsertvations after these ocrrections:

- 1) Apply Zolotov et al. (2012) prescription for  $V_{1kpc}$  reduction;
- 2) Subhalos that have a <20kpc pericenter passage and lose 90% of their mass are considered disrupted;
- 3) Subhalos must exceed zdependent mass threshold (Okamoto et al. 2008) to allow gas to cool and form stars.

### **Baryonic Effects on Dark Matter**

#### Two Examples:

1) A Baryonic Solution to "Too Big To Fail"

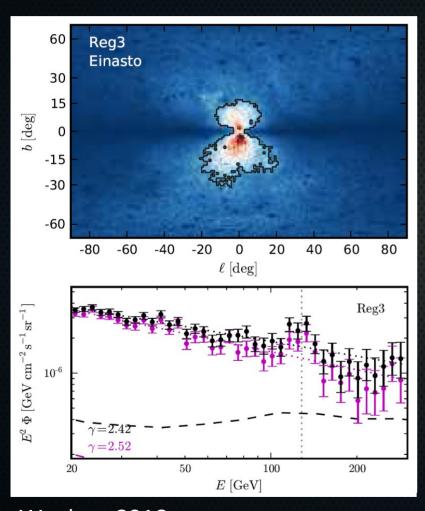
Brooks, Kuhlen, Zolotov, & Hooper (2012), arXiv:1209.5394

2) An Offset Dark Matter Density Peak in the Galactic Center?

Kuhlen et al. (2012), arXiv:1208.4844

#### III. Baryonic Effects on DM at the Galactic Center

#### **130 GeV Line from the Galactic Center**



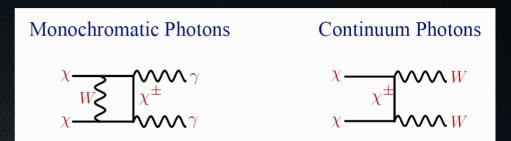
Residual map 2.0 1.5 Cm .0 0.0 -45 -0.5 -90 -180 180 GC spectrum ( $\psi_o < 4^\circ$ ,  $|b| > 0.5^\circ$ ) GC spectrum ( $\theta > 40^{\circ}$ ) E2 dN/dE [arb. units] E [GeV]

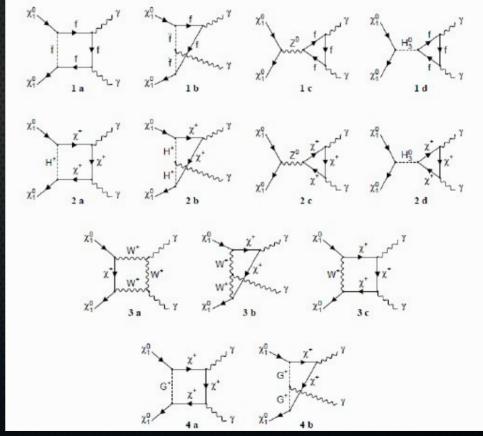
Weniger 2012

Su & Finkbeiner 2012

#### DM annihilation?

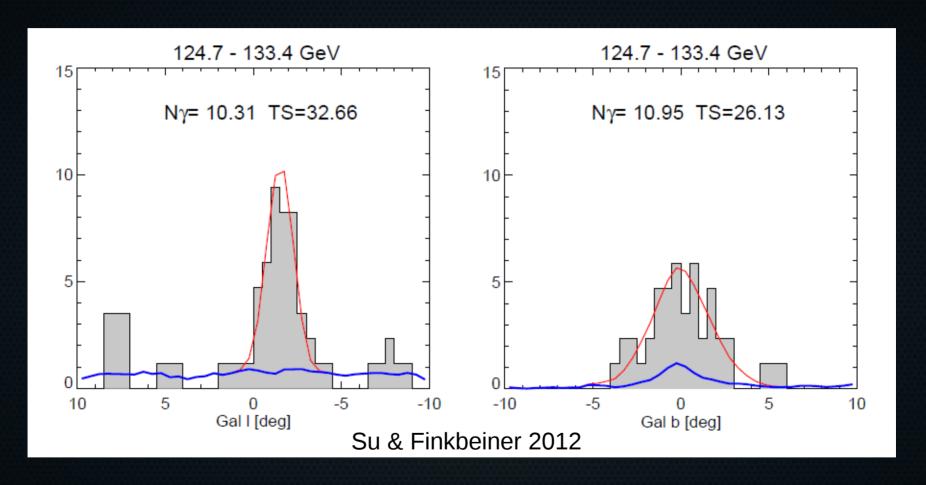
- 2-body annihilation:  $\chi \chi \to \gamma \gamma$ ,  $\gamma Z$ ,  $\gamma h$
- Normally "loop suppressed"  $(10^{-2} 10^{-4})$  compared to continuum radiation.
- But models with enhanced lines exist, e.g.: Singlet DM (Profumo et al. 2010)
   "Higgs in Space" (Jackson et al. 2010)





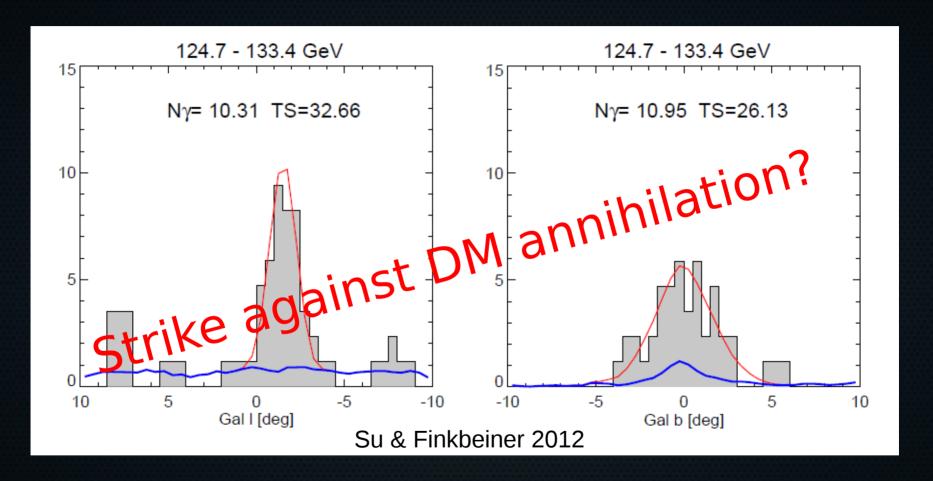
Bergström & Ullio 1997

# The line is not exactly at the Galactic Center



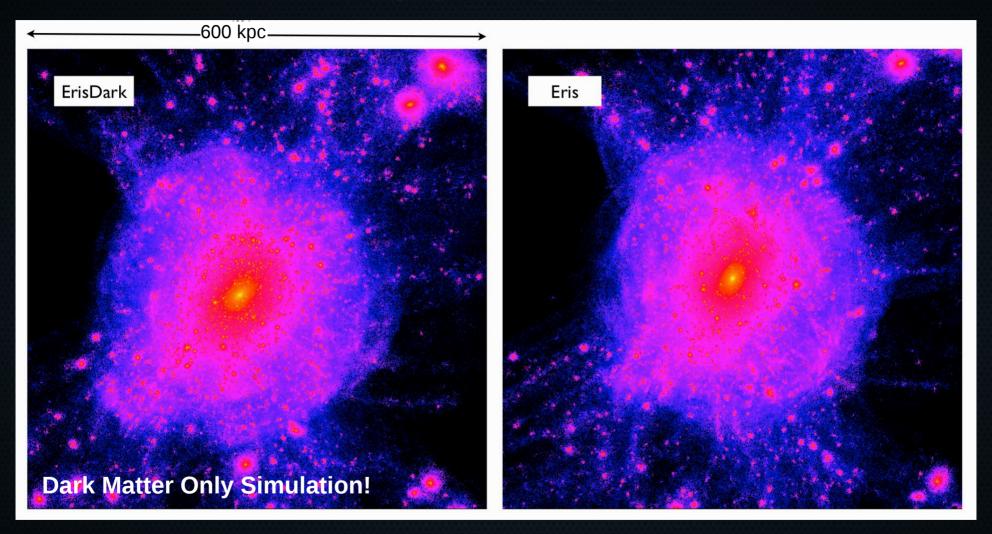
The significance of the signal is maximized at  $(\ell,b) = (-1.5^{\circ},0^{\circ})$ , or about **200 projected pc** from Sgr A\*.

# The line is not exactly at the Galactic Center



The significance of the signal is maximized at  $(\ell,b) = (-1.5^{\circ},0^{\circ})$ , or about **200 projected pc** from Sgr A\*.

### Eris & ErisDark

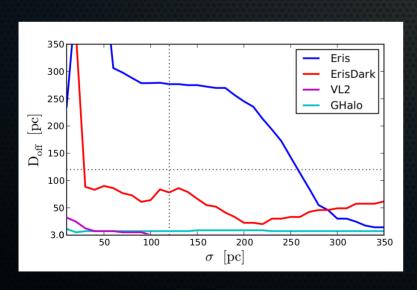


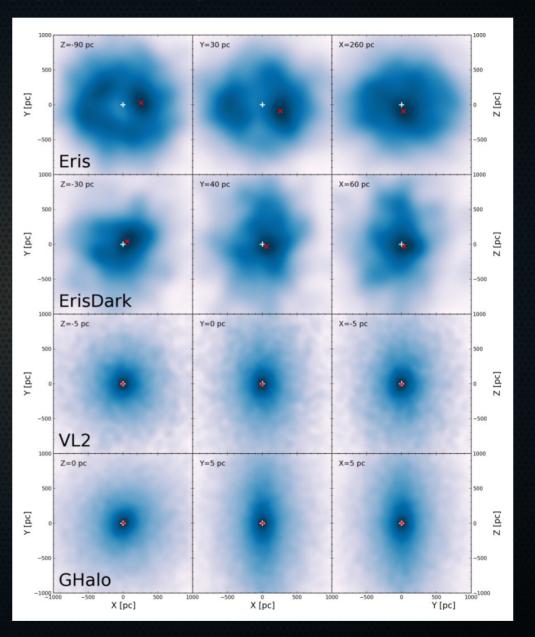
ErisDark has the same initial conditions as Eris, except that all of the matter is treated as dark matter. (Pillepich et al., in prep.)

#### DM offset in Eris

In the dissipational simulation (Eris), the maximum of the DM density is displaced from the minimum of the potential (dynamical center).

The DM-only runs show no such offset (to within one grav. softening length).



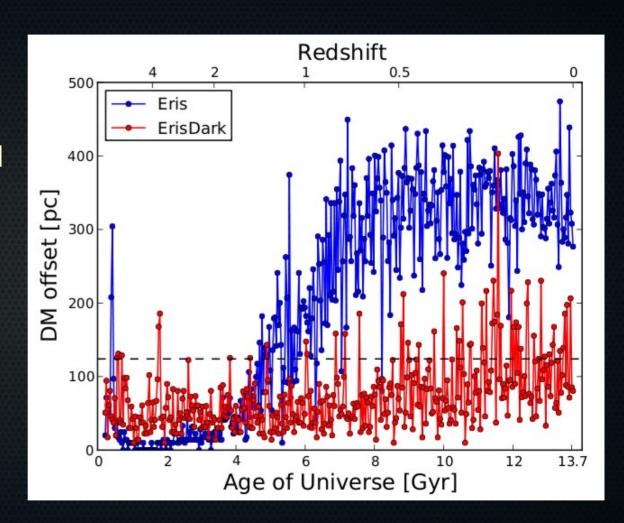


#### Formation and Evolution of the Offset

The offset is no fluke – it appears around z=1.5 and persists afterwards.

$$<$$
D<sub>off</sub> $> = 340$  pc (almost 3  $\epsilon_{soft}$ ).

In ErisDark the offset remains below  $\sim 1\epsilon_{soff}$ .



#### Formation and Evolution of the Offset

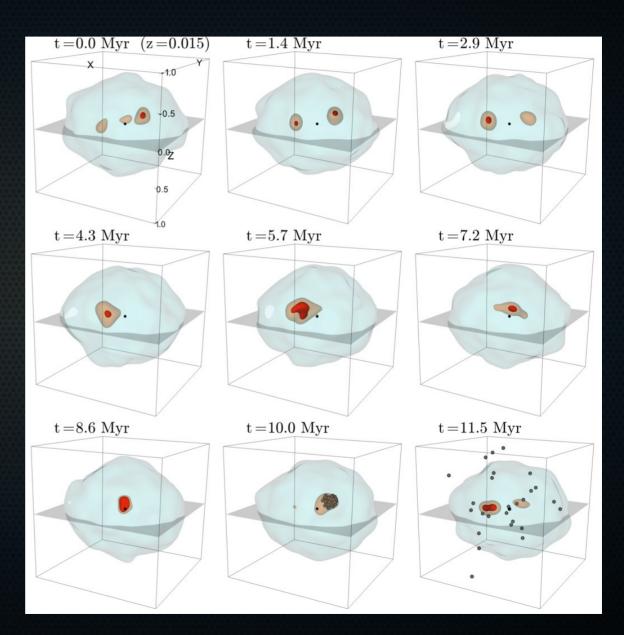
Eris output are spaced ~35 Myr – too long for dynamical analysis.

High output cadence re-run of the last few hundred Myr of Eris.

Typically close to the disk plane:

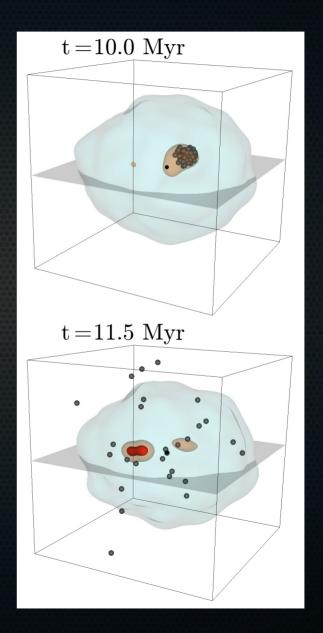
$$<\Delta R> = 340 \pm 51 \text{ pc}$$
  
 $<\Delta z> = 64 \pm 46 \text{ pc}$ 

Not stationary.
Not coherent.
Sometimes multiple peaks.



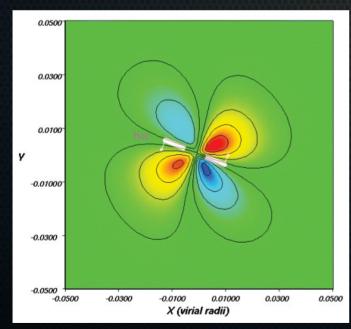
Particles within 1  $\epsilon_{\text{soft}}$  of the offset peak at one time are no longer part of the offset peak as short as 1.5 Myr later.

Not a coherent, bound structure. Not an incompletely disrupted subhalo.

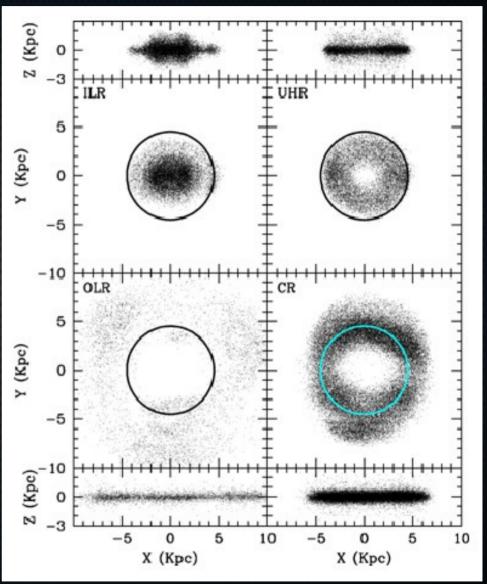


# Resonant interaction with the stellar bar?

At times Eris has a very pronounced stellar bar. Maybe orbital resonances could lead to a density-wave-like excitation?



Weinberg & Katz 2002, 2007

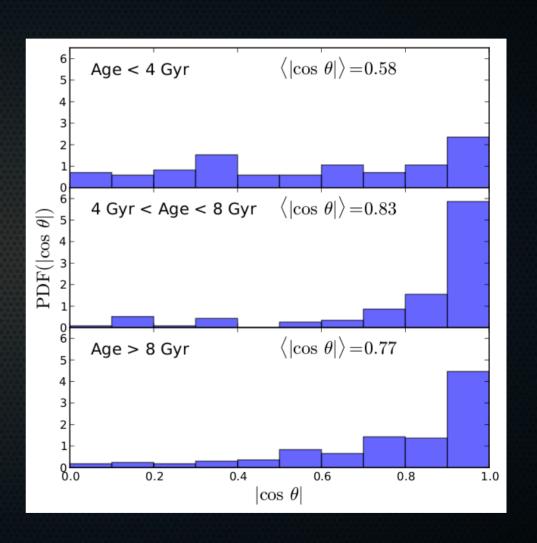


Ceverino & Klypin 2007

Resonant interaction with the stellar bar?

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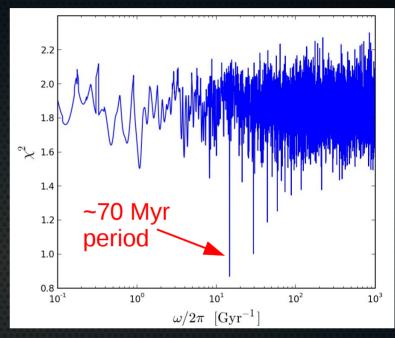
The direction of the DM offset is aligned with the orientation of the stellar bar in Eris.

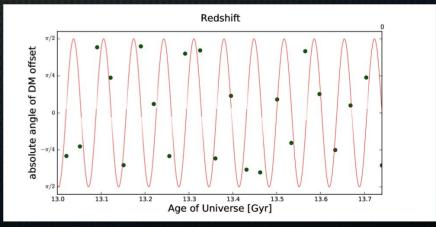


# Resonant interaction with the stellar bar?

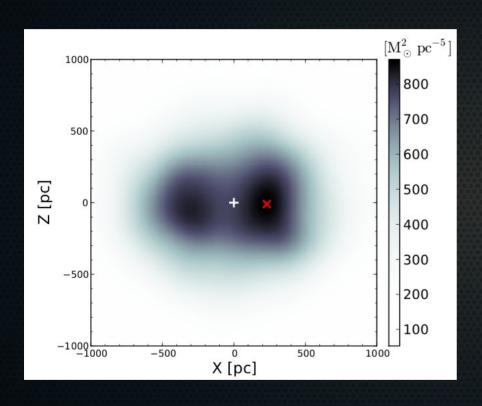
At times Eris has a very pronounced stellar bar. Maybe orbital resonances could lead to a density-wave-like excitation?

The angle in the disk plane to the offset shows periodic behavior.





# DM annihilation implications?



At the resolution of the Eris simulation the contrast in DM annihilation surface brightness between the peak and the Galactic Center is only ~10-15%.

Such a low contrast is not compatible with a DM annihilation interpretation of the 130 GeV line.

# HOWEVER: WE DO NOT RESOLVE THE OFFSET PEAK!

The contrast may increase with higher resolution...

#### Conclusions

- ➤ Ultra-high resolution DM simulations of Galactic structure predict enormous amounts of substructure, both in configuration space (subhalos) and in velocity space (streams, debris flow).
- This substructure has important consequences for astro-physical probes of DM, and indirect (annihilation) and direct (nuclear scattering) detection experiments.
- Cold and collisionless DM-only simulations by themselves are nearing the end of their usefulness.

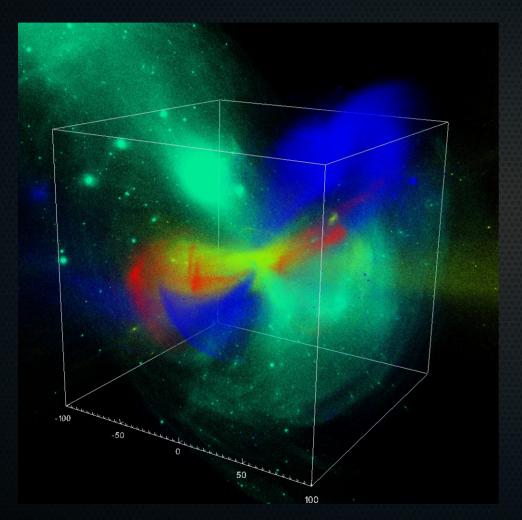


- ➤ Baryonic physics is too important to neglect on small scales. Results are uncertain due to treatment of hydrodynamics and prescription of cooling, star formation, and especially feedback physics.
- Often even the sign of the effect (e.g. adiabatic contraction vs. cusp-to-core transformation) is unknown.
- Nevertheless, important progress is being made (e.g. Eris simulation), and are highlighting some important modification to expectations from DM-only simulations. Two examples:
  - 1) A Baryonic Solution to Too Big To Fail
  - 2) An Offset DM Density Peak at the Galactic Center

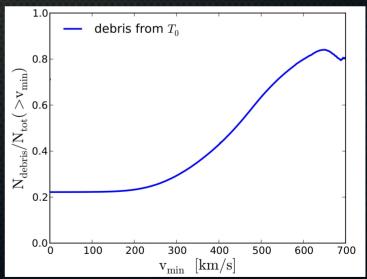
#### **Extra Slides**

#### **Debris Flow**

"Debris Flow" = Any material that was bound to a subhalo at z>0 and is no longer bound to it at z=0.



6
5
4
2
1
0
100 200 300 400 500
v (km/s)

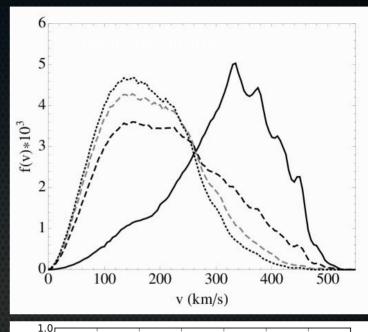


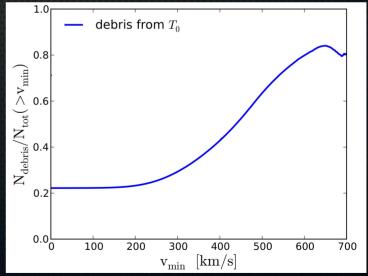
Kuhlen, Lisanti, & Spergel (2012)

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Kuhlen, Lisanti, & Spergel (2012)

# Beyond Cold & Collisionless DM-only Simulations

Cold and Collisionless DM-only Simulations [Millennium II, Via Lactea II, Aquarius, etc.]

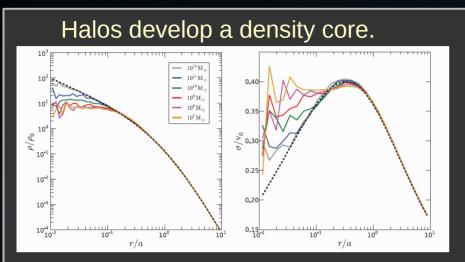
#### Alternative Dark Matter Physics

Warm Dark Matter Self-Interacting Dark Matter ???

#### Include Baryonic Physics

Gas Cooling
Star Formation
Feedback

### **Alternatives: Self-Interacting Dark Matter**

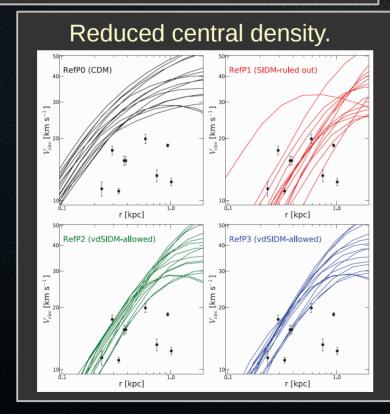


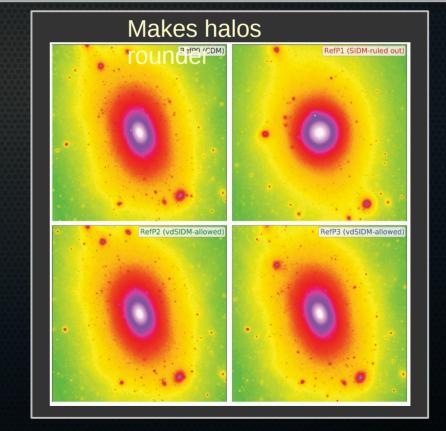
Vogelsberger, Zavala, & Loeb (2012) See also Rocha, Peter, et al. (2012)

Velocity-dependent scattering cross section:

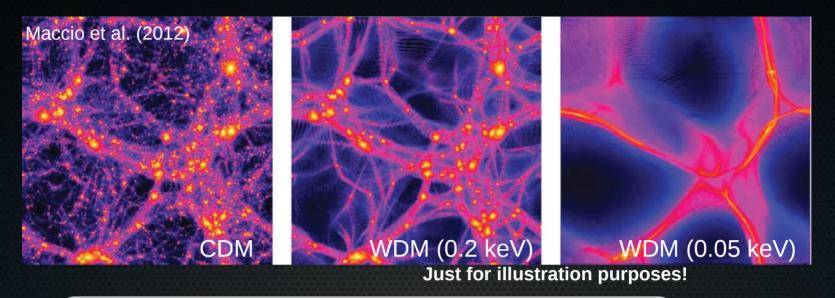
$$\frac{\sigma_{\rm T}}{\sigma_{\rm T}^{\rm max}} \approx \begin{cases} \frac{4\pi}{22.7} \beta^2 \ln(1+\beta^{-1}), & \beta < 0.1, \\ \frac{8\pi}{22.7} \beta^2 (1+1.5\beta^{1.65})^{-1}, & 0.1 < \beta < 10^3, \\ \frac{\pi}{22.7} \left( \ln\beta + 1 - \frac{1}{2} \ln^{-1}\beta \right)^2, & \beta > 10^3, \end{cases}$$

Feng, Kaplinghat, & Yu (2010), Finkbeiner et al. (2011), Loeb & Weiner (2011)

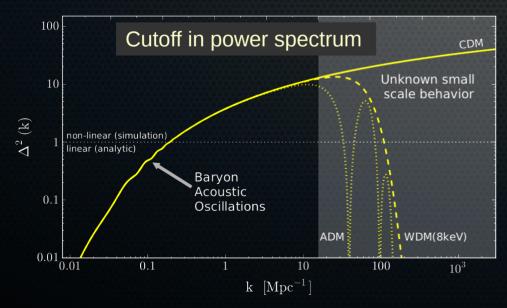


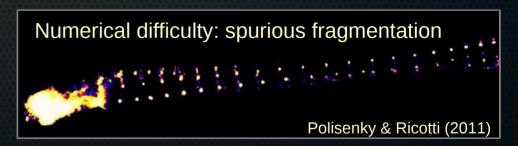


#### **Alternatives: Warm Dark Matter**



Observational Limits from Ly- $\alpha$  forest:  $m_{WDM} > 2 - 4$  keV. (Viel et al. 2006, 2008; Abazajian 2006; Seljak et al. 2006)

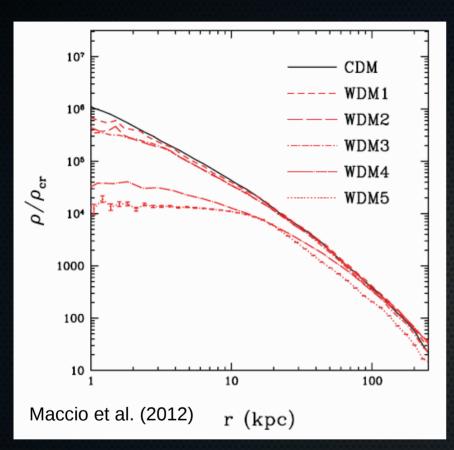


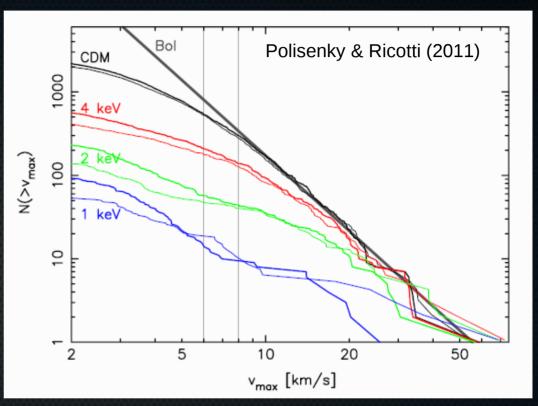


See also: Bode et al. (2001), Gao & Theuns (2007), Lovell et al. (2011), Maccio et al (2012)etc.

UC Berkeley Colloquium

#### **Alternatives: Warm Dark Matter**





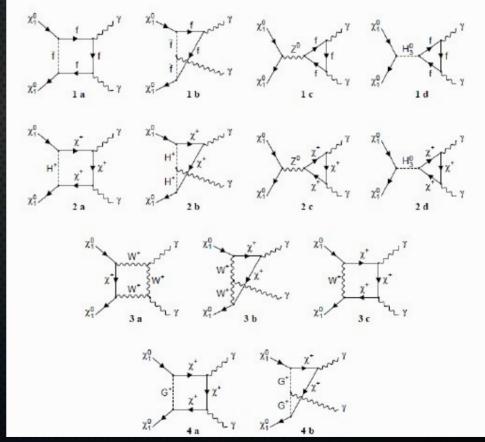
Catch-22: either you get cores, but not enough subhalos, or you can match the ultra-faint dwarfs, but then you don't get big enough cores.

Villaescusa-Navarro & Dalal (2011), Maccio et al. (2012)

#### **DM annihilation?**

- 2-body annihilation:  $\chi\chi \to \gamma\gamma$ ,  $\gamma Z$ ,  $\gamma h$
- Normally "loop suppressed"  $(10^{-2} 10^{-4})$  compared to continuum radiation.
- But models with enhanced lines exist, e.g.: Singlet DM (Profumo et al. 2010)
   "Higgs in Space" (Jackson et al. 2010)





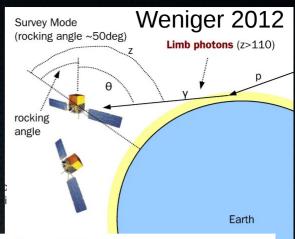
Bergström & Ullio 1997

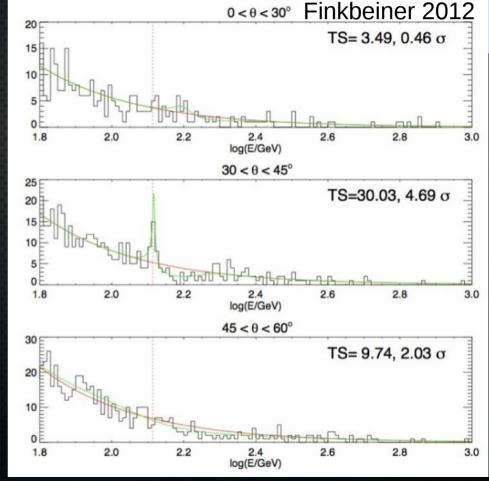
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#### **Instrument systematics?**

• Earth limb photons of intermediate incidence angle show a similar line...





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#### **Astrophysical explanations?**

- Broken power-law mimics line? (Profumo & Linden 2012)
- Inverse Compton in the Klein-Nishina regime with ~130 GeV mono-chromatic electrons from multiple pulsars? (Aharonian et al. 2012)

# 

Fig. 1. Colour: energy spectra of the inverse Compton radiation of mono-energetic electrons upscattering isotropic target photons for 4 different values of the parameter b: 1, 7, 50 and 100. The energy of gamma-rays is in units of the electron energy. Grey: the gamma-ray spectrum produced by electrons with relativistic Maxwellian distribution; in this case the photon energies are in units of  $4\Theta$ , where  $\Theta$  is the "temperature" of Maxwellian distribution.